

# An Economic Theory Masterclass

## Part II: The Supply and Demand Paradigm

Lones Smith

March 3, 2020

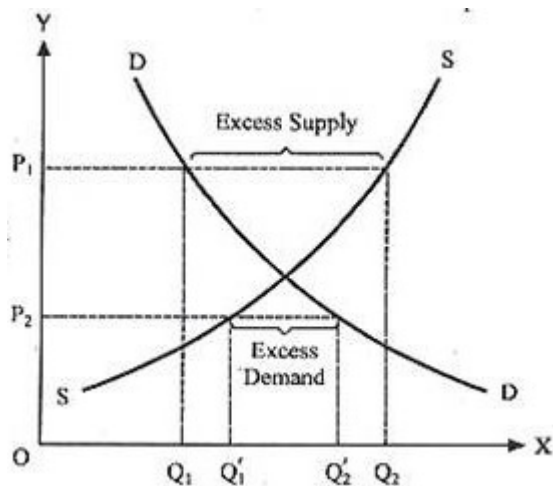
# The Supply and Demand Paradigm

- ▶ We consider a competitive price-taking environment summarized by a (usually upward sloping) supply curve and (usually downward sloping) demand curves.
- ▶ Each curve reflects both extensive and intensive margins.
- ▶ These two curves answer out-of-equilibrium hypothetical “what if” questions: what would the supply and demand be at any other price?
- ▶ By parsing our logic into supply and demand, we can compartmentalize our analysis, and make clearer predictions

# Stability — Does Competitive Equilibrium Happen?

- ▶ Supply price and quantity:  $P_S$  and  $Q_S$
- ▶ Demand price and quantity:  $P_D$  and  $Q_D$
- ▶ If the world is changing, should market equilibrium arise?
- ▶ We explore the adjustment *tatonnement process* (“groping”)
- ▶ Walrasian price stability
  - ▶ price adjustment process of fictional double auctioneer
  - ▶ If *net demand* is positive at some price, then the price rises
  - ▶ If net demand is negative, then the price decreases
  - ⇒ change in the price shares the sign of  $Q_D - Q_S$ .
  - ▶ Source: Leon Walras, *Elements of Pure Economics* (1874)
- ▶ Marshallian quantity stability
  - ▶ If demand price exceeds supply price at some quantity, then supply quantity rises, and conversely
  - ▶ Suppliers raise/reduce supply of high/low demand goods
  - ⇒ change in the quantity shares the sign of  $P_D - P_S$ .

# Walrasian and Marshallian Stable



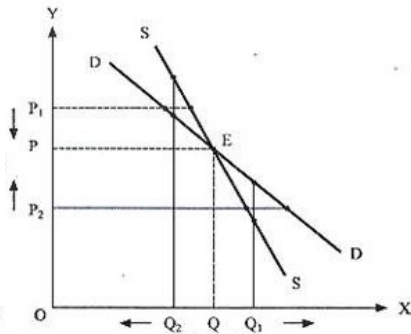
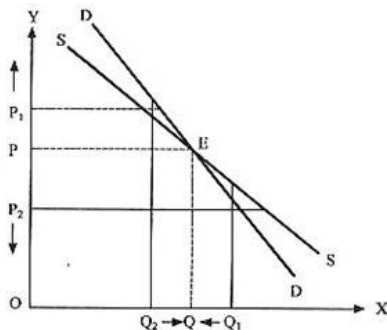
# Stability with Linear Supply and Demand

- ▶ linear supply  $P_S = a_S + b_S Q_S$  and demand  $P_D = a_D - b_D Q_D$ .
- ▶ Demand slopes down:  $b_D > 0$ . So when  $P_D = P_S = P$ , we have

$$Q_D - Q_S = \frac{a_D}{b_D} + \frac{a_S}{b_S} - P \left( \frac{1}{b_D} + \frac{1}{b_S} \right)$$

- ▶ Walrasian price stability:
    - ▶  $Q_D - Q_S$  falls in  $P$  at  $P_D = P_S = P$ , or  $1/b_D + 1/b_S > 0$ .
  - ▶ Marshallian quantity stability:
    - ▶  $P_D - P_S = a_D - a_S - (b_D + b_S)Q$  falls in  $Q$  iff  $b_D + b_S > 0$
  - ▶ Both hold with falling demand and rising supply ( $b_D, b_S > 0$ )
  - ▶ But if the supply curve slopes down,
    - ▶ Walrasian price stability holds iff  $b_D < |b_S|$
    - ▶ Marshallian quantity stability holds iff  $b_D > |b_S|$
- ⇒ for a slightly backward bending supply curve,  $|b_S|$  is large, and so equilibrium is Walrasian but not Marshallian stable.

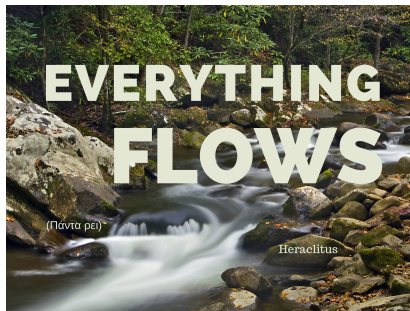
# Stability: Downward-sloping Demand and Supply



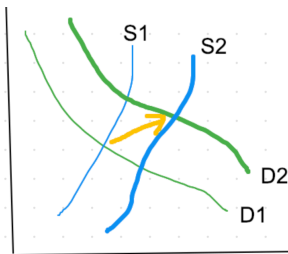
- ▶ demand steeper than supply  $\Rightarrow$  Walrasian unstable and Marshallian stable
- ▶ supply steeper than demand  $\Rightarrow$  Walrasian stable and Marshallian unstable

# Comparative Statics Analysis

- ▶ Supply and demand are not just static notions
- ▶ Units are per week, or per day, etc.
- ▶ Dynamics: Heraclitus — [Panta Rhei](#)
  - ▶ “All entities move and nothing remains still”
- ▶ “No man ever steps in the same river twice”



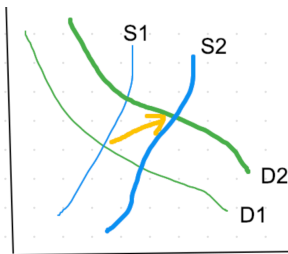
# Comparative Statics Analysis



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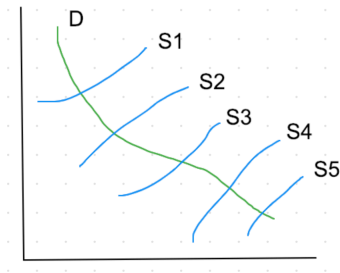
# Comparative Statics Analysis



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⇒ comparing the two static situations is informative
- ▶ Famous counter example: “overshooting” model of Dornbusch (1976) in international finance (cited 6600 times)
  - ▶ After an unexpected influx of new money, the domestic price level adjusts slowly, but the exchange rate can adjust quickly.
  - ▶ Convergence to new steady-state is nonmonotone (overshoots)

# Identification of Supply and Demand Curves

- ▶ price and quantity reflect both supply and demand.
- ▶ If you wanted to “identify” the demand curve, you find something that just shifts supply and leaves demand invariant.
- ▶ With enough variation in supply, we can identify the demand.
- ▶ Likewise, variation in demand but not supply would allow one to pin down the supply curve.



# Elasticities Review

- ▶ Review: More elastic supply or demand has larger quantity response for any price change
  - ▶ Change is proportionate:  $\varepsilon = (dQ/dP)(P/Q)$
- ⇒ Elasticity is unit-free!
- ▶ When  $|\varepsilon| > 1$ , we call the supply or demand **elastic**
  - ▶ Demand elasticity is spoken of in absolute terms!

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**Answer**: Upward sloping linear supply curves
- ▶ **Q2**: Characterize constant elasticity falling demand curves.

# Elasticities Review

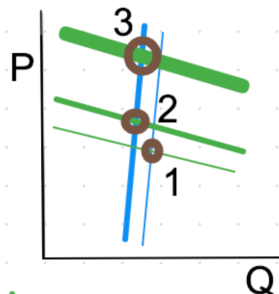
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**Answer: Upward sloping linear supply curves**
- ▶ **Q2: Characterize constant elasticity falling demand curves.**  
**Answer: Hyperbolic downward sloping curves:  $P = Q^{1/\varepsilon}$**

# Large Price Volatility in the Oil Market

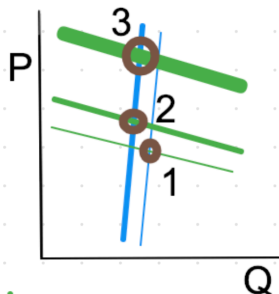
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  - ▶ Huge price volatility
  - ▶ Minimal quantity volatility
  - ▶ Slow change in fundamentals





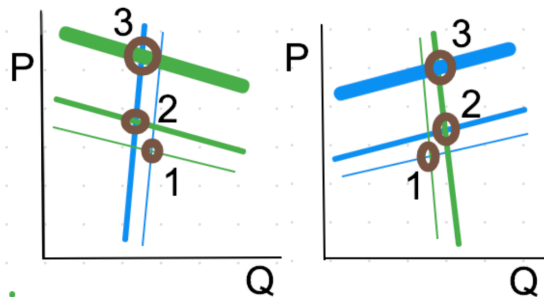
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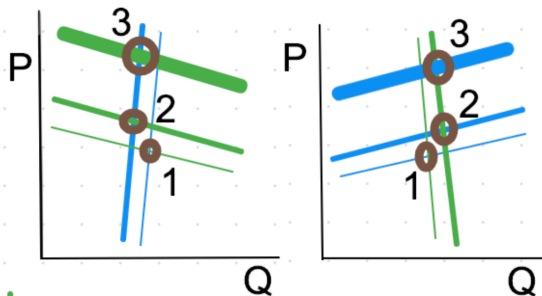
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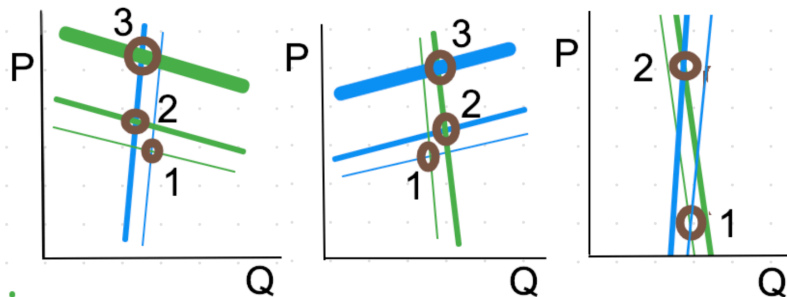
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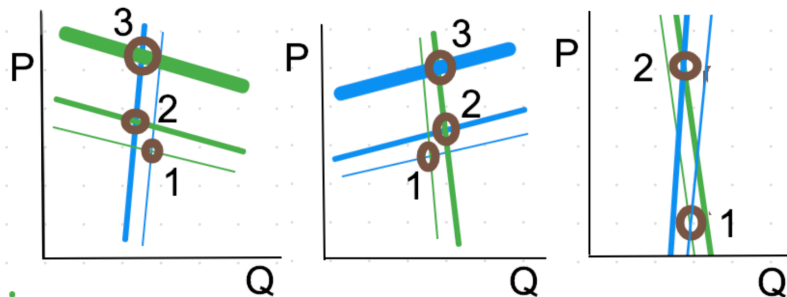
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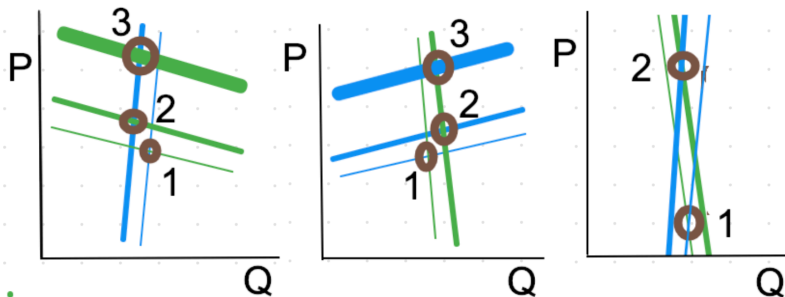
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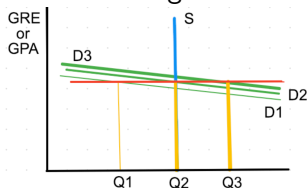
- ▶ Lesson 1: Small fundamentals shifts cause large proportionate price changes iff both supply and demand are highly inelastic.
- ▶ Lesson 2: Inelastic supply or demand  $\Rightarrow$  low quantity volatility

# Large Quantity Volatility

- ▶ Lesson 3: Small fundamentals changes can lead to large quantity changes iff supply and demand are highly elastic.
- ▶ Lesson 4: Elastic supply or demand  $\Rightarrow$  low price volatility

# Large Quantity Volatility

- ▶ Lesson 3: Small fundamentals changes can lead to large quantity changes iff supply and demand are highly elastic.
- ▶ Lesson 4: Elastic supply or demand  $\Rightarrow$  low price volatility
- ▶ College admissions is an “implicit market”, where the “price” is the admission bar (Try to formalize why this is true.)
- ▶ Source: Chade, Lewis, and Smith (2014), “Student Portfolios and the College Admissions Problem” (in canvas)

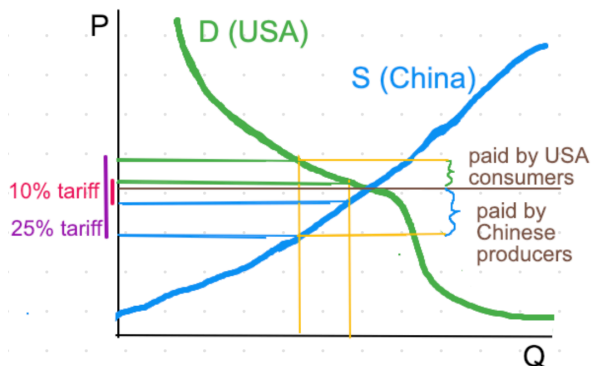


- ▶ Without waitlisting, as in PhD admissions, acceptance bar mistakes can lead to massive changes in acceptance rates.
- ▶ 2017: UC-Irvine unadmitted 499 students



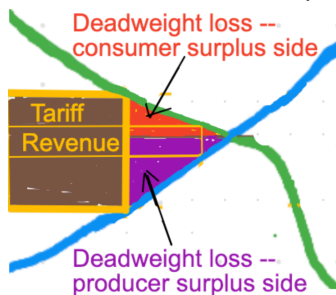
# Shared Incidence or Tax or Tariff

- ▶ Trump added a 10% tariff on Chinese imports, to rise to 25%
- ⇒ wedge between supply and demand prices:  $P_D > P_S$ .
- ▶ Incidence: Who pays the tariff or tax?
- ▶ “China is paying us billions of dollars in tariffs.” — Trump



# Deadweight Loss of Tax

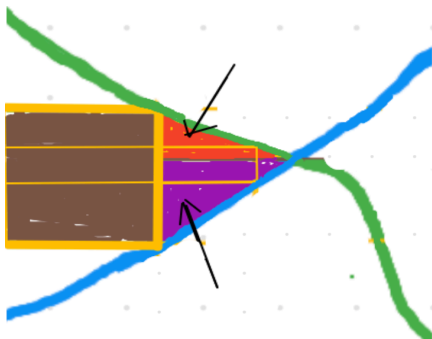
- ▶ Double auctions: No effect of small tax! Here: small effect.
  - ▶ Lost gains from trade = lost consumer + producer surplus
  - ▶ Assume tariff revenue is socially neutral: gain to government balances loss to producers or consumers
- ⇒ deadweight loss (excess burden) of tariff is red + purple
- ▶ Tariff revenue rises proportionately less than the tariff rise



← Taxes erase marginal trades

# Changes in the Deadweight Loss of Tax

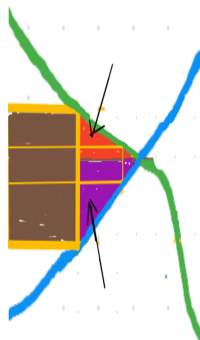
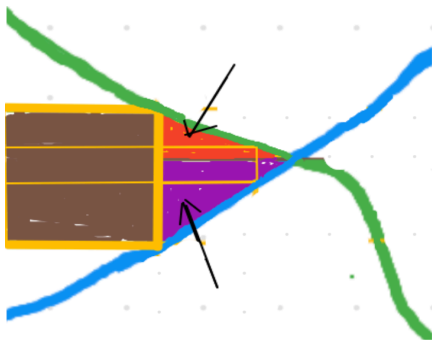
- ▶ The deadweight loss of a tariff increases in the quantity reduction, larger with more inelastic demand or supply



(more elastic S and D)  
(longrun?)

# Changes in the Deadweight Loss of Tax

- ▶ The deadweight loss of a tax increases in the quantity reduction, larger with more inelastic demand or supply



(less elastic S and D)  
(shortrun?)

# Optimal Taxes: the Ramsey Inverse Elasticity Rule

- ▶ Tax revenue falls when the tax rises if the demand is elastic:

$$[Q(P + \tau)\tau]' = Q(P + \tau) + Q'(P + \tau)\tau = Q(P + \tau)[1 + \varepsilon \frac{\tau}{P + \tau}]$$

$\Rightarrow$  never tax an elastically demanded good

- ▶ Optimal taxes seek to minimize deadweight losses, and so focus on inelastically demanded or supplied goods.
- ▶ Ramsey (1927): Minimize the social cost of raising revenue  $R$

$$\max V(p + \tau, I) \text{ s.t. } \tau \cdot x(p + \tau, I) \geq R$$

- ▶ **Ramsey inverse elasticity rule:**  
“taxes should be proportional to the sum of the reciprocals of its supply and demand elasticities”
- ▶ In other words, governments should not tax elastically demanded goods or elastically supplied goods.



# Optimal Taxes

- ▶ Governments know to tax inelastically supplied resources:
  - ▶ Oil taxes, mineral taxes
  - ▶ existence tax: poll tax (head tax) in Britain (fertility impact?)
  - ▶ wealth taxes are usually real estate, or at death taxes
  - ▶ millionaire tax? billionaire tax?

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- ▶ More rationality  $\leftrightarrow$  more elastic response
  - ▶ Example: Does income reflect effort, ability, luck or networks?
  - ▶ Tax luck or ability or networks — inelastically supplied.
  - ▶ “The harder I work, the luckier I get.” — Sam Goldwyn

# Taxes — Basic Accounting Insights

- ▶ Tariff or sales or *ad valorem* tax:  $P_D(Q) = P_S(Q) + \tau P_S(Q)$
- ▶ *Specific tax*  $\tau$ :  $P_D(Q) = P_S(Q) + \tau$
- ▶ Wisconsin specific tax examples
  - ▶ gas tax: state 32.9¢ and federal 18.4¢ per gallon
  - ▶ Beer: 6¢/gallon and wine: 25¢/gallon and liquor: \$3.25/gallon
  - ▶ Also exists for cigarettes
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## Theorem (Tax Irrelevance Theorem)

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## Theorem (Tax Irrelevance Theorem)

*Regardless of whether demand or supply pays the tax, the demand and supply prices, market quantity, and efficiency loss are the same.*

- ▶ Specific tax is easier to analyze: parallel demand / supply shift

# Tax Incidence and Elasticities

- Incidence: The more inelastic side of the market pays more of a tax and benefits more from a subsidy
- Demand elasticity  $\varepsilon = (dQ_D/dP_D)(P_D/Q_D) < 0$
- Supply elasticity  $\eta = (dQ_S/dP_S)(P_S/Q_S) > 0$

## Theorem (Incidence Theorem)

*The share of a small tax paid by demand is  $\frac{\eta}{\eta - \varepsilon} \leq 1$ .*

- *Proof:* Impose a small excise tax  $\tau \equiv P_D - P_S > 0$
- Markets clear:  $dQ_S/Q = dQ_D/Q$ .

$$\Rightarrow \quad \eta \frac{dP_S}{P_S} = dQ_S/Q = dQ_D/Q = \varepsilon \frac{dP_D}{P_D}$$

$$\Rightarrow \quad \tau = dP_D - dP_S = dP_D - \frac{\varepsilon}{\eta} \frac{dP_D}{P_D} P_S \approx dP_D - \frac{\varepsilon}{\eta} dP_D$$

since  $P_D/P_S = (P_S + \tau)/P_S \approx 1$  with error similar size to  $\tau$

$$\Rightarrow dP_D \approx \frac{\eta}{\eta - \varepsilon} \tau > 0 \quad \text{and} \quad dP_S \approx \frac{\varepsilon}{\eta - \varepsilon} \tau < 0$$

# Deadweight Loss for Small Taxes

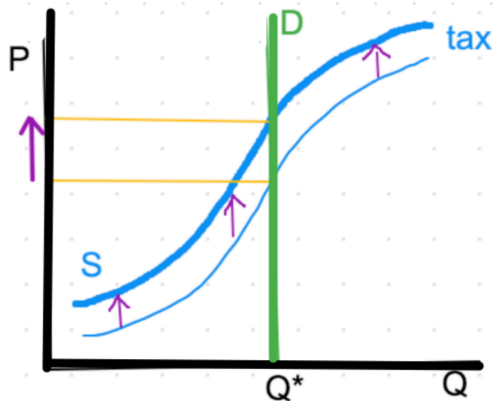
- ▶ Since  $\varepsilon = (dQ_D/dP_D)(P_D/Q_D)$ , the quantity changes by

$$dQ = \epsilon \frac{dP_D Q}{P_D} \approx \epsilon \left( \frac{\eta}{\eta - \epsilon} \right) \tau \left( \frac{Q}{P_D} \right) = \left( \frac{1}{\frac{1}{\epsilon} - \frac{1}{\eta}} \right) \tau \left( \frac{Q}{P_D} \right)$$

- ▶ Hence, the deadweight loss is the area of the standard triangle:

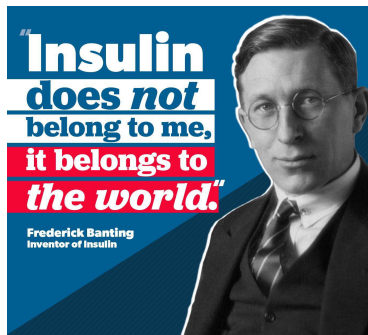
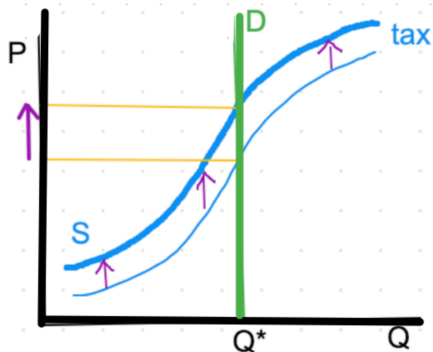
$$\frac{1}{2}(dQ)(dP_D - dP_S) = \frac{1}{2}(dQ)\tau = \left( \frac{1}{\frac{1}{\epsilon} - \frac{1}{\eta}} \right) \left( \frac{Q}{2P_D} \right) \tau^2$$

## Impact of an Insulin Tax



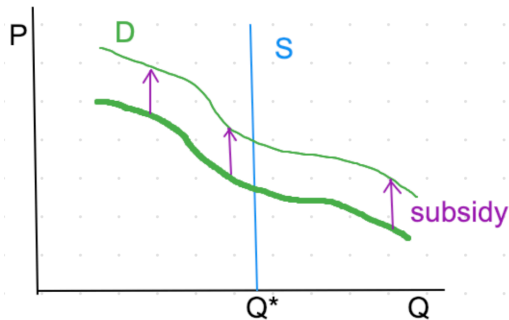
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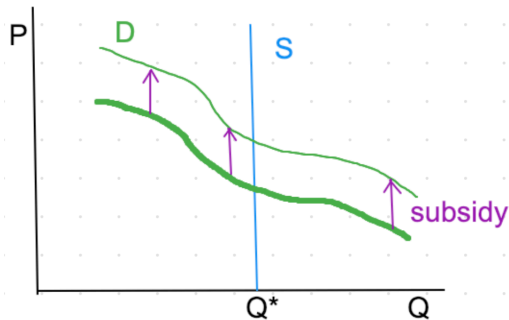
- ▶ By the tax incidence theorem, we can apply the tax to supply
- ▶ There is no deadweight loss of the tax, as  $Q = Q^*$  fixed!
- ▶ In fact, insulin was sold for \$1 by Canadians Banting and Best to the University of Toronto.
- ▶ insulin has new patents, and its price has leapt up!

# Michigan College Subsidy Eliminated



- ▶ In 2009, Michigan ended the Promise Scholarship program, giving 96,000 in-state students up to \$4,000 for college
- ▶ Who fought to keep it? Colleges!

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- ▶ Another fixed supply context: the “death effect” for artists
- ▶ Hyperinflations



# Application of Supply and Demand to Rollover Lotteries

- ▶ A *classic lottery* has a unique winner with a fixed prize.
- ▶ In a **Genoese lottery**, people pick their own numbers: If no one wins, the prize rolls over; if many win, the prize is shared.
- ▶ Why do people gamble? Consider a quasi-linear model: People gamble if the expected utility of winnings plus the thrill of playing the lotto exceeds the ticket price.
- ▶ Rollovers can identify this model.
- ▶ Assume risk neutrality.
- ▶ Let  $M$  denote the number of possible lotto numbers (“odds”), and so the winning chance for the jackpot is  $1/M$ .
  - ▶  $M \approx 259000000$  for Megamillions
  - ▶  $M \approx 292000000$  for Powerball.
- ▶ Ticket price  $p$  and lottery taxes  $\tau \in (0, 1)$
- ▶ Let  $J$  denote the remaining jackpot of last period.
- ▶ Classic lotto prize of  $W$

## Expected Lotto Winnings

- ▶ Assume  $S$  tickets sold for a drawing (our quantity)
- ⇒ The expected number of winners is  $\mu = S/M$ .
- ▶  $Q(k|M, S) = P(k \text{ winners}) = C(S, k)(1/M)^k(1 - 1/M)^{S-k}$
- ▶ Accounting for expected gains from the classic lotto and possibly shared jackpot among  $S$  ticket buyers:

$$\begin{aligned} E(\text{ticket winnings}) &= W/S + \frac{1}{M} \sum_{k=0}^S \frac{J + p(1 - \tau)S}{k + 1} Q(k|M, S - 1) \\ &\approx W/S + [J/S + p(1 - \tau)][1 - e^{-S/M}] \end{aligned}$$

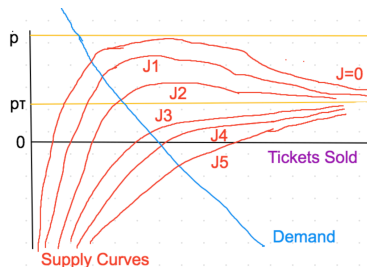
(using the Poisson approximation to the Binomial)

- ▶ We will rephrase this as the “supply” of expected ticket losses:

$$E(\text{ticket losses}) = p - W/S - [J/S + p(1 - \tau)][1 - e^{-S/M}]$$

- ▶ We treat this as an implicit market where the expected losses from tickets as the “net price” of thrill of the lotto experience.

# Supply Curve of Lotto Losses, as the Jackpot Rises



- ▶ The supply curves shift down as the jackpot rises, and is negative for large jackpots.
- ▶ Each supply curve asymptotes to  $p\tau$  as  $S \uparrow \infty$
- ▶ More sold tickets
  - (a) inflates the next jackpot, which depresses supply losses
  - (b) raises the prize sharing chance, increases supply losses
- ▶ The demand curve is the locus of lotto losses for the thrill
- ▶ Rollovers just shift the supply curve and so identify demand

# Supply / Demand Curves: Intensive and Extensive Margins

- ▶ We introduced the supply and demand in the double auction
- ▶ There, all gains from trade — namely, producer plus consumer surplus — reflect heterogeneity.
- ▶ We now allow a realistic intensive margin,
  - ▶ Output from every firm, and consumption from every consumer, increases in the market price
  - ▶ the producer surplus also increases in cost convexity, and consumer surplus increases in preference convexity
- ▶ We just flesh out the logic for supply curves

# Supply Curves: Intensive and Extensive Margins

- ▶ A cost is **escapable** if can be avoided.
  - ▶ Otherwise, it is inescapable or “sunk”.
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  - ▶ Marginal costs  $\Leftrightarrow$  intensive margins
  - ▶ Average costs  $\Leftrightarrow$  extensive margins

# Short, Medium, Long Runs

- ▶ We use static models to capture dynamic notions
- ▶ As the run increases, there are more choice margins, and so inescapable costs  $\rightsquigarrow$  escapable (e.g., rental contracts end).
- ▶ **Short run**
  - ▶ fixed costs are inescapable; cost function is just variable costs
  - ▶ Insufficient time for entry; reducing output to zero
- ▶ **Long run**
  - ▶ All costs are escapable, and so are included in the cost function
  - ▶ firms enter if there are profits to be made and otherwise exit
  - ▶ John Maynard Keynes: “In the long run we are all dead”
  - ▶ JMK: ignoring dynamics (eg. quantity theory of money) unwise
- ▶ **“Medium run”**
  - ▶ more decision margins available, and so more costs escapable, than in the short run, and fewer than in the long run.

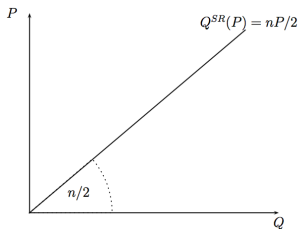


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- ▶ **Industry supply curve**
  - ▶ price-quantity locus  $(P, Q)$ , such that, the allowable firms — i.e., the existing firms in the short run, or all potential firms in the long run — profitably produce  $Q$  **taking price  $P$  as given**
  - ▶ Note: price-taking behavior is incredible with few firms

## Example of Supply with Homogeneous Firms

- ▶ Cost functions  $C(q) = 1 + q^2$  (fixed cost 1 & variable cost  $q^2$ )
- ▶ Optimal production:  $P = C'(q) = 2q \Rightarrow$  output  $q = P/2$ .
- ▶ Short run supply with  $n$  firms:  $Q_n^{SR}(P) = nq = nP/2$  🤖



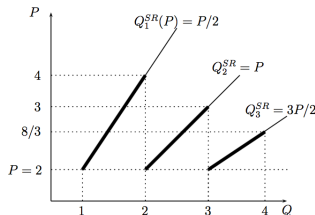
- ▶ The supply curve rises simply due to cost convexity.
- ▶ The source of all profits is cost convexity (diminishing returns)
- ▶ This intensive margin effect — firms sell more with a higher price — was not present with double auctions

# Sawtooth Long Run Supply

- ▶ For the long run, firms earn nonnegative profits with all costs escapeable, and no firm wishes to enter or exit.
- ▶ Entry  $\Rightarrow$  long run supply is more elastic (Le Chetalier)
- ▶ The least price needed for production is 2, since:

$$C'(q) = P \geq C(q)/q = \frac{1}{q} + q \Rightarrow 2q \geq \frac{1}{q} + q \Rightarrow q \geq 1 \Rightarrow P \geq 2 \text{ 🤔}$$

- ▶ Just after entry, all firms earn zero profits (equal quantities)
- ▶ So 🤯 and 🤔  $\Rightarrow Q_n^{SR}(P) \geq n(2/2) = n$  and  $P_{n-1}^{SR}(P) \leq 2\frac{n}{n-1}$
- ▶ The long run supply curve is therefore a **sawtooth curve**



The supply curve is not the cheapest way to produce any given quantity. Indeed, two firms produce  $q = \sqrt{2}$  as cheaply as one:  
 $1 + (\sqrt{2})^2 = 2[1 + (\sqrt{2}/2)^2]$

## Example — Supply with Heterogeneous Firms

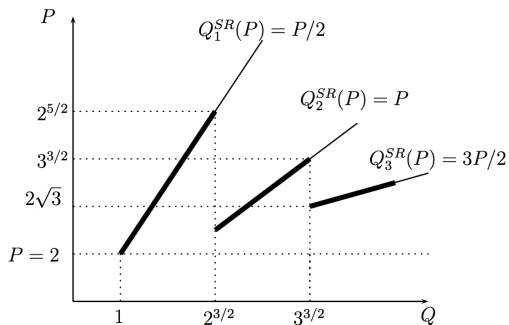
- ▶ Firm  $n$  has the cost function  $C_n(q) = n + q^2$ , for  $n = 1, 2, \dots$
- ▶ So supply is unchanged at 🤖:  $Q_n^{SR}(P) = nq = nP/2$ .
- ▶ For the long run, since the fixed cost is escapable (variable), each firm now has different average costs. For firm  $n$ , we have

$$MC = P \geq C(q_n)/n = \frac{n}{q} + q \Rightarrow 2q \geq \frac{n}{q} + q \Rightarrow q \geq \sqrt{n} \Rightarrow P \geq 2\sqrt{n} \text{ 😬}$$

⇒ the least quantity is  $Q_n^{SR}(2\sqrt{n}) = n(2\sqrt{n})/2 = n\sqrt{n}$  😬

- ▶ Only the marginal firm now earns zero profits.
- ▶ Inframarginal firms earn positive profits
  - ▶ = returns to a fixed factor, like a location or other fixed asset.
  - ▶ If this asset is properly priced, the accounting profits disappear.

# Sawtooth Long Run Supply with Heterogeneous Firms



The supply curve now rises due to cost convexity and heterogeneity

- ▶ Repeatedly applying the supply curve quantity ranges 🤪, and sawtooth prices rising from  $2\sqrt{n}$  (😬) to  $2\sqrt{n} \cdot 2/(n-1)$  (😱)
- ▶  $n = 1$ :  $P_S(Q) = 2Q$  on  $[1, 2\sqrt{2}]$  from  $P = 2$  to  $P = 4\sqrt{2}$ .
- ▶  $n = 2$ :  $P_S(Q) = Q$  on  $[2\sqrt{2}, 3\sqrt{3}]$  from  $P = 2\sqrt{2}$  to  $P = 3\sqrt{3}$
- ▶  $n = 3$ :  $P_S(Q) = 2Q/3$  on  $[3\sqrt{3}, 4\sqrt{4}]$  from  $P = 2\sqrt{3}$  to ...